

Transition between Bending and shear failure for RC Beams without shear reinforcement

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INVESTIGATION OF $V_{\min}$

- Eurocode shear formula:

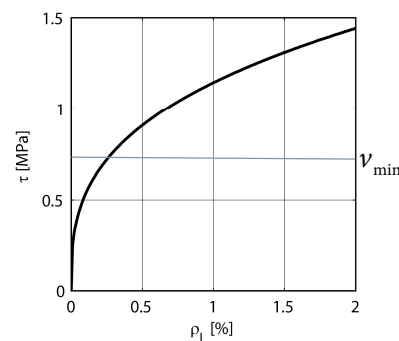
$$V_{Rd,c} = [C_{Rd,c} k (100 \rho_l f_{ck})^{1/3} + k_1 \sigma_{cp}] b_w d$$

$$V_{Rd,c} = (v_{\min} + k_1 \sigma_{cp}) b_w d$$

with

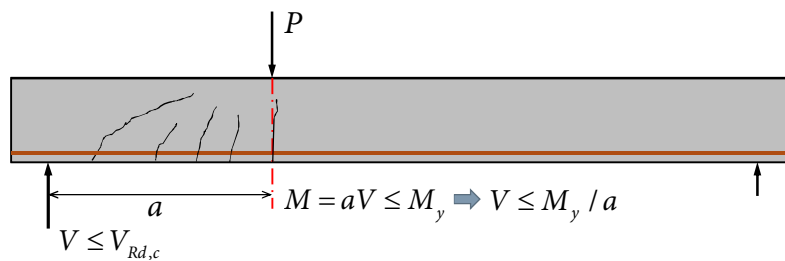
$$v_{\min} = 0.035 k^{3/2} f_{ck}^{1/2}$$

$$k = 1 + \sqrt{\frac{200}{d}} \leq 2.0$$



$V_{MIN} \rightarrow V_{bd}$

- The minimum average shear stress that can cause a shear failure before the yielding of flexural reinforcement



V_{MIN} IN EC2

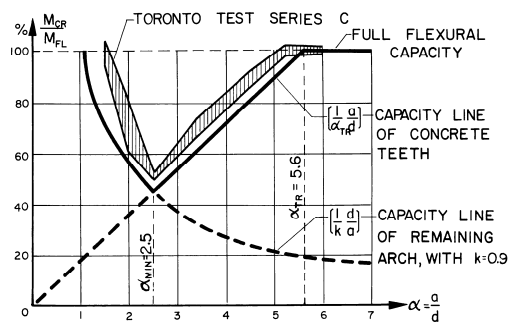
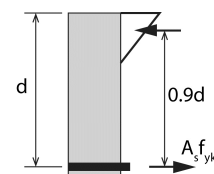
- Bending failure criterion

$$V \leq M_y / a$$

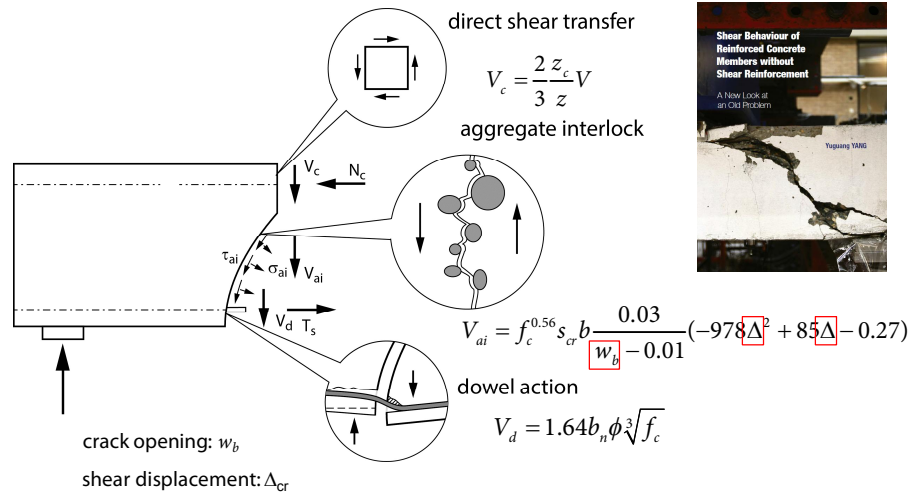
with

$$M_y = A_s f_{yk} (0.9d)$$

$$a = 2.5d$$



V_{MIN} BASED ON A PHYSICAL MODEL



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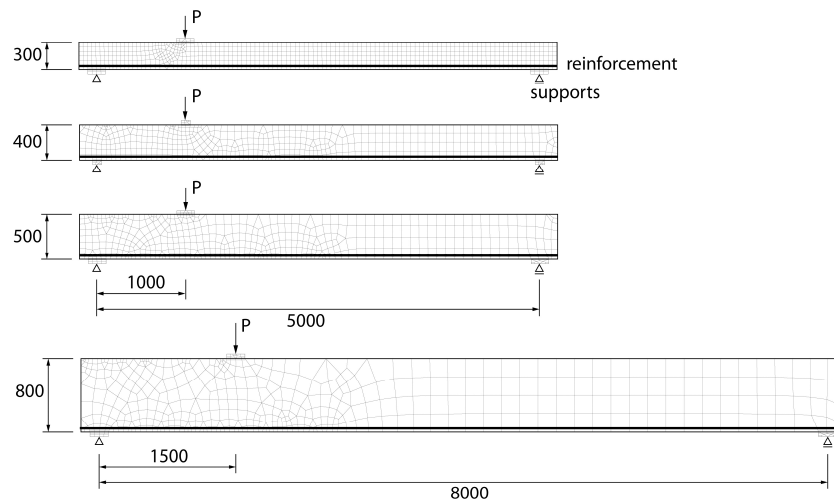
FEM STUDIES – VARIABLES

- Beam depth d , $d = 255, 355, 455$ or 755 mm
- Concrete strength f_{cm} , $f_{cm} = 34$ or 68 MPa
- Reinforcement ratio ρ
- Shear slenderness ratio a/d

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FEM – MESHES



FEM – MODEL CONFIGURATIONS

- Concrete properties based on FEM guideline and Model Code 1990
- Smearred crack model, fixed crack model

Low Strength Concrete	
Compressive strength f_{cm}	= 34.0 MPa
Tensile strength f_{ctm}	= 2.81 MPa
Elastic Modules E_c	= 34.0 GPa
Fracture Energy G_f	= 70.2 N/m

High Strength Concrete	
Compressive strength f_{cm}	= 68.0 MPa
Tensile strength f_{ctm}	= 4.46 MPa
Elastic Modules E_c	= 42.6 GPa
Fracture Energy G_f	= 111.4 N/m

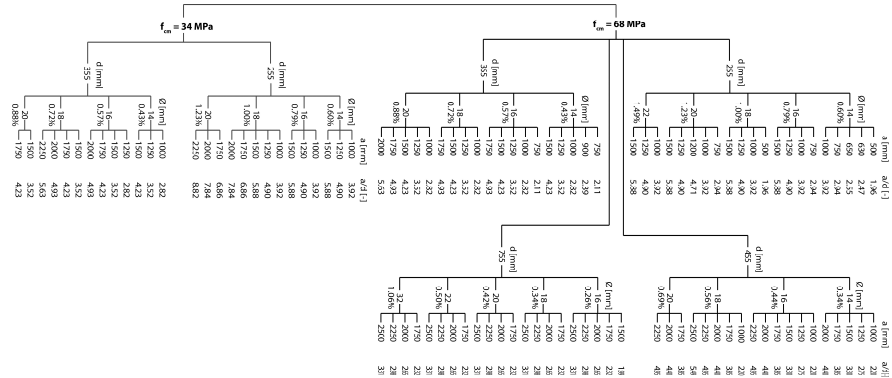
$$w = \frac{6}{1 + 120} \frac{w}{16 + D_{max}}$$

$$\sqrt{j_{cm}}$$

Modified Compressive
Field Theory, Colins
et.al.

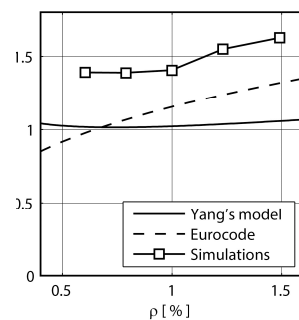
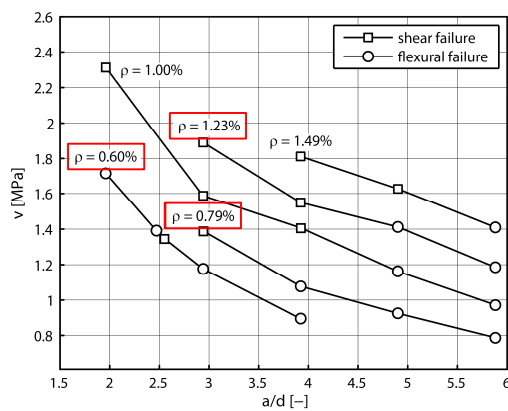
FEM-MODELS

- 115 models



PREDICTIONS

- $d = 260 \text{ mm}$, $f_{cm} = 68 \text{ MPa}$



EXPERIMENTAL PROGRAM

- Variables
 - Reinforcement ratio ρ_l
 - Concrete strength f_{cm}
 - Beam depth d

EXPERIMENTAL PROGRAM

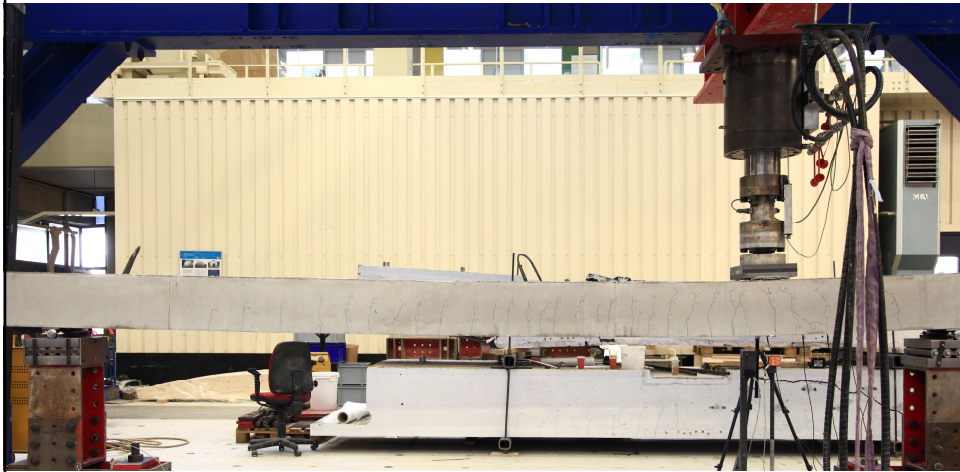
- Series 1: 8 beams with 4 reinforcement ratios

f_{cm} [MPa]	h [mm]	rebar config.	r [%]	M_y [kN·m]	V_{EC} [MPa]
70	300	1 Ø10 + 2 Ø16	0.60%	69.4	0.97
70	300	3 Ø16	0.75%	87.0	1.05
70	300	1 Ø12 + 2 Ø20	0.93%	106.0	1.13
70	300	3 Ø20	1.18%	134.4	1.22

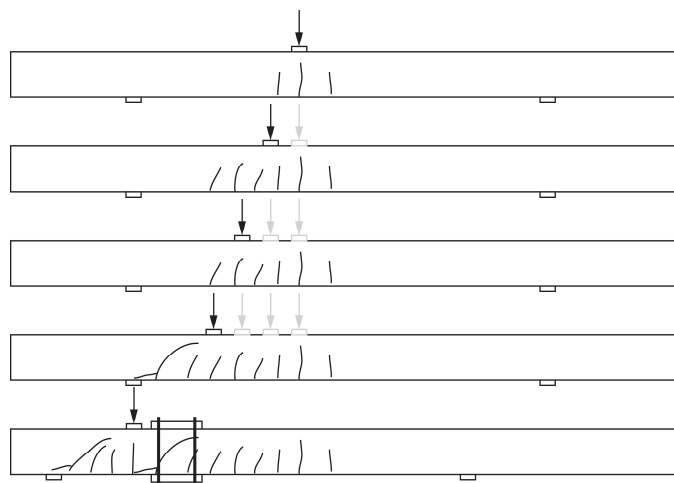
- Series 2: 10 beams with different concrete strength and beam depth

f_{cm} [MPa]	h [mm]	rebar config.	r [%]	M_y [kN·m]	V_{EC} [MPa]
40	300	3 Ø12	0.44%	44.5	0.73
40	300	3 Ø16	0.75%	87.0	0.87
40	300	1 Ø12 + 2 Ø20	0.93%	106.0	0.94
70	500	2 Ø16 + 1 Ø20	0.49%	167.9	0.81
70	500	3 Ø20	0.64%	237.1	0.90

TEST SETUP

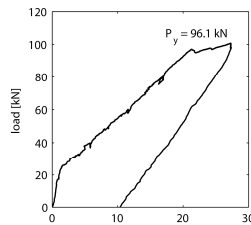


EXPERIMENTAL PROGRAM

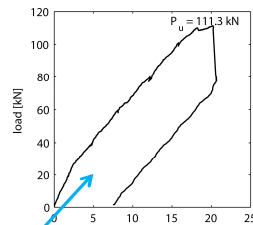


RESULTS

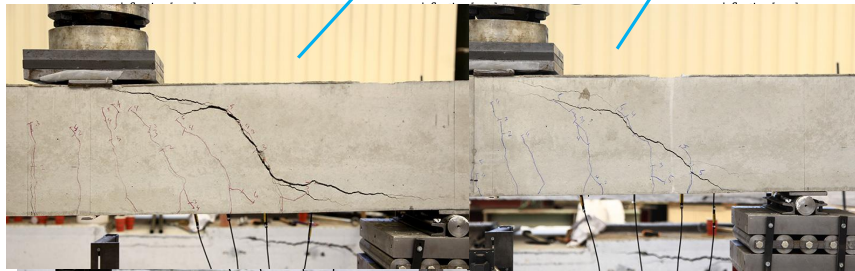
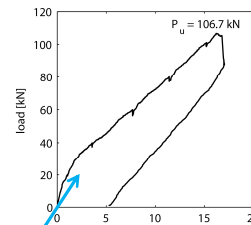
Bending: A751A1



Shear + bending: A751B1



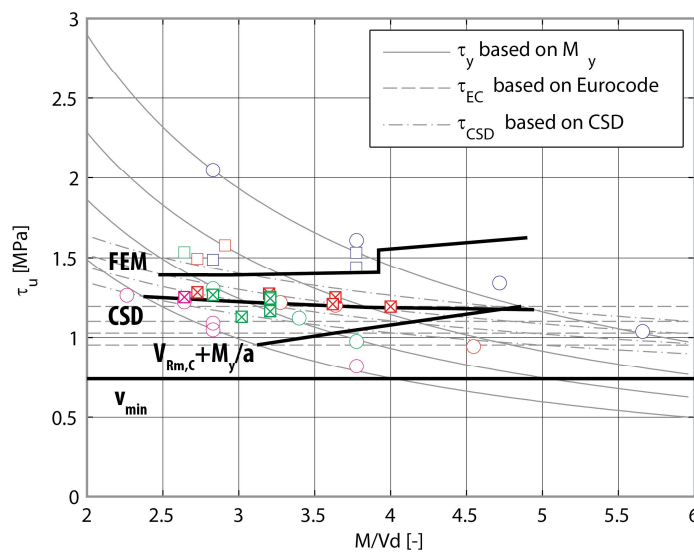
Shear: A751B2



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RESULTS

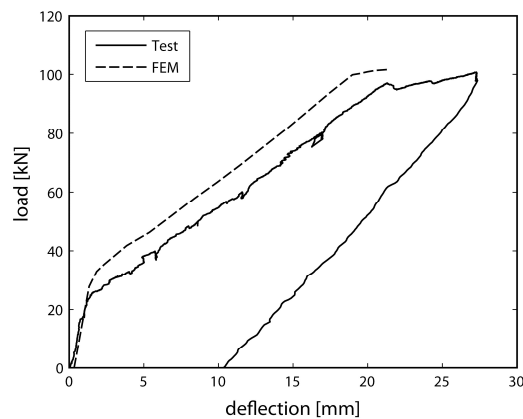


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COMPARISON WITH TEST RESULTS

- A751A1: $a = 1000$ mm, $3\varnothing 16$ mm bars



RWS NLFEA SAFETY FORMAT

- Global Resistance Factor Method (GRF)

$$f_{cm} = 0.85 f_{ck} \quad f_{ym} = 1.1 f_{yk} \quad P_d = P_u / \gamma_{GL}$$

- Partial Safety Factor Method (PF)

$$f_{cd} = f_{ck} / \gamma_{RD} \gamma_c \quad f_{ctd} = f_{ctk} / \gamma_{RD} \gamma_c \quad \dots$$

$$P_d = P_u$$

- Estimation of COV of resistance (ECOV)

$$P_d = P_u / \gamma_{RD} \gamma_R \quad \gamma_R = e^{\alpha_R \beta V_R} \quad V_R = \frac{1}{1.65} \ln \left(\frac{P_{u,m}}{P_{u,c}} \right)$$

RWS NLFEA SAFETY FORMAT

- Global Resistance Factor Method (GRF)

$$f_{cm} = 51 \text{ MPa} \quad f_{ym} = 550 \text{ MPa}$$

- Partial Safety Factor Method (PF)

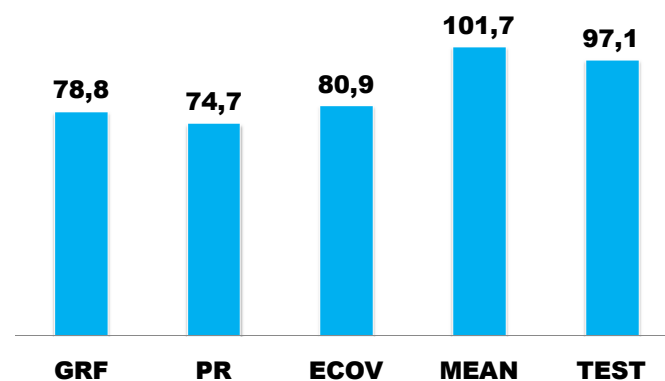
$$f_{cd} = 38 \text{ MPa} \quad f_{yd} = 410 \text{ MPa}$$

- Estimation of COV of resistance (ECOV)

$$f_{ck} = 60 \text{ MPa} \quad f_{yk} = 500 \text{ MPa}$$

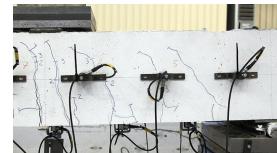
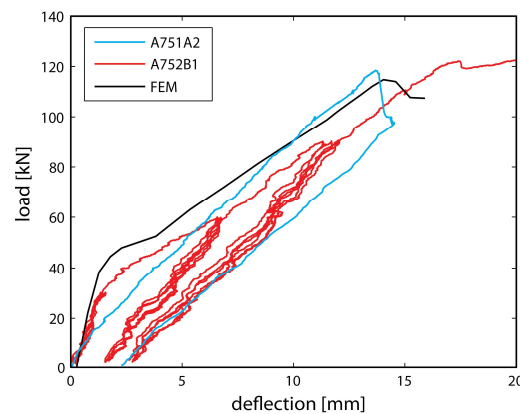
COMPARISON WITH TEST RESULTS

- All the simulations are bending failure



COMPARISON WITH TEST RESULTS

- A751A2 & A751B1: $a = 750$ mm

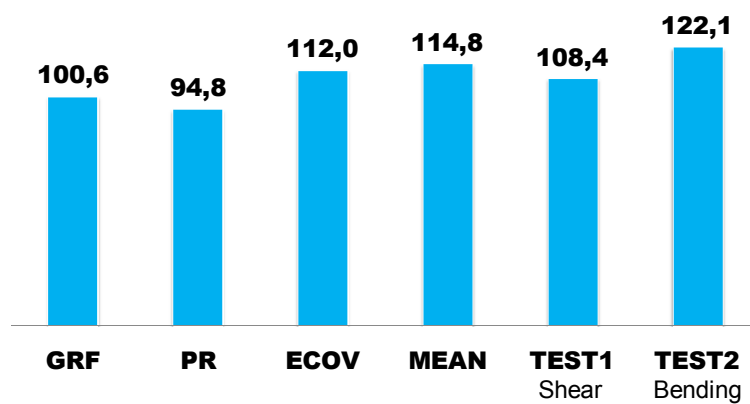


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COMPARISON WITH TEST RESULTS

- Only with mean values shear failure is found.



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COMPARISON WITH TEST RESULTS

- Switch of failure mode

$$P_{u,m} = 114.8 \text{ kN} \quad P_{u,c} = 116.9 \text{ kN}$$

$$V_R = \frac{1}{1.65} \ln \left(\frac{P_{u,m}}{P_{u,c}} \right) < 0 \quad \gamma_R < 1.0$$

$$P_d = P_u / \gamma_{RD} \gamma_R$$

CONCLUSIONS

- The CSD models gives quite accurate prediction on $v_{\min}$
- NLFEA gives reasonable prediction when using the mean values of material properties
- The safety format has to be carefully interpolated when the failure model is changing

Thanks for your attention.